

The ecology of Roman trade. Reconstructing provincial connectivity with similarity measures

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Abstract

The creation of the Roman Empire promoted the connectivity of a vast area around the Mediterranean sea. Mobility and trade flourished over the Roman provinces as massive amounts of goods were shipped over thousands of kilometres through sea, rivers and road networks. Several works have explored these dynamics of interaction in specific case studies but there is still no consensus on the intensity of this connectivity beyond local trade.

We argue here that the debate on the degree of large-scale connectivity across the empire is caused by a lack of appropriate methods and proxies of economic activity. The last years have seen an improvement on the availability of evidence as a growing amount of datasets is collected and published. However, data does not equal knowledge and the methods used to analyse this evidence have not advanced at the same pace.

A new framework of connectivity analysis has been applied here to reveal the existence of distinctive trade routes through the provinces of the Western region of Rome. The amphora stamps collected over more than a thousand sites have been analysed using quantitative measures of similarity. The patterns that emerge from the analysis highlight the intense connectivity derived from factors such as the spatial closeness, presence of military units and the relevance of the Atlantic sea as a main shipping route.

Keywords: Rome, trade, amphora stamps, MRPP, Jaccard

1. Introduction

The intensity of provincial connectivity is one of the most debated aspects of the Roman economy. Hypotheses oscillate be-

tween a unified market defined by a constant flow of goods through long-range trade to isolationist approaches based on autonomous regions with little contact, with some exceptions (Temin, 2001; Bang, 2007). Both archaeological and written sources indicate that there was a large diversity of scenarios as connectivity was not homoge-

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13 neous and some regions were much more 56
14 integrated than others. A key player of 57
15 this integration was the Roman army as its 58
16 supply required the import of vast quan- 59
17 tities of products (Scheidel et al., 2007, 60
18 591). They were mostly produced in spe- 61
19 cialised provinces and required large-scale 62
20 trade. A good example of this connectivity 63
21 is the shipping of massive amounts of olive 64
22 oil from the Baetican province to Britan- 65
23 nia after its conquest (Remesal Rodríguez, 66
24 2011, 60). These basic goods were dis- 67
25 tributed amongst military garrisons but 68
26 it seems probable that the trade network 69
27 rapidly expanded to supply civilian settle- 70
28 ments (Williams and Peacock, 1983). Other 71
29 goods such as exotic foods were widely 72
30 shipped to distant urban centres using non- 73
31 military redistribution networks (Livarda 74
32 and Orengo, 2015; Orengo and Livarda, 75
33 2016). However, the general question re- 76
34 mains unanswered: how frequent and in- 77
35 tense were these economical contacts be- 78
36 yond specific case studies? 79

37 The topic has a renewed interest as 80
38 an increasing corpus of datasets includ- 81
39 ing archaeological, epigraphical and written 82
40 sources is becoming available. One exam- 83
41 ple of this exciting explosion of evidence is 84
42 the Orbis project which is focused on ex- 85
43 ploring the cost of mobility along the entire 86
44 Roman Empire (Scheidel, 2015). Other ini- 87
45 tiatives such as the Pelagios project aims at 88
46 aggregating tens of different databases to 89
47 generate a multifaceted view of the classi- 90
48 cal world (Barker et al., 2016). This col- 91
49 lection of evidence is a critical step towards 92
50 understanding the Roman economy but its 93
51 use also presents several challenges (Bow- 94
52 man and Wilson, 2009, 3-87). As other au- 95
53 thors have pointed out this data is riddled 96
54 with biases and uncertainty up to the point 97
55 where it is difficult to find patterns beyond 98

the noise (Bevan, 2014; Wilson, 2009). The
datasets being merged often have diverse
temporal and spatial dimensions and were
collected by different formats and methods
while the projects creating them use differ-
ent theoretical approaches to the past (Be-
van, 2015; Calvanese et al., 2016).

The aim of integrating datasets should
be combined with the creation of methods
able to tackle the complexities of the ex-
isting evidence (Brughmans and Poblome,
2016). Roman studies typically use de-
scriptive statistics and linear regressions to
analyse relations between variables (Wil-
son, 2009) but these generic approaches
were not designed to face the uncertainty
of archaeological data. First, our sample
sizes are usually very low as they consist
of tens or hundreds of data points for a
vast region that did not remain stable over
time. Second, the data points have a large
degree of uncertainty which is badly cap-
tured by exploratory methods and require
the use of probabilistic approaches to the
past (Yubero-Gómez et al., 2016; Crema,
2015; Bevan et al., 2013a,b). Finally, the
multiple biases generated by the archaeo-
logical process should be taken into account
while analysing the existing evidence (Be-
van, 2012; Rubio-Campillo et al., 2012).

This work presents a method to study
provincial connectivity through the estima-
tion of similarity indexes. The premise
of this analysis is that regions that share
trade routes should exhibit more similar cul-
tural traits between them than with the
rest of the empire. We reconstruct here
the dynamics of provincial trade based on
a well-tested proxy of long-range trade: the
stamps found in amphorae containers found
over the entire Roman Empire (Scheidel
et al., 2007, 690). By applying a Null-
Hypothesis Significance Testing Framework

99 based on ecological methods we explore two 140
100 specific research questions: a) was large- 141
101 scale trade related to the provincial struc- 142
102 ture? and b) can we find patterns of con- 143
103 nectivity between provinces beyond spatial 144
104 closeness? 145

105 The next two sections define the dataset 146
106 and the methods we used for this large-scale 147
107 analysis. The fourth section presents the 148
108 results of the analysis which are discussed 149
109 and interpreted in section five. The text 150
110 finishes with a summary of the method and 151
111 its potential contribution within the current 152
112 debates on the discipline. 153

113 2. Patterns of trade in the Roman em- 155 114 pire 156

115 Clay amphorae are arguably the archae- 158
116 ological artefacts that best represent trade 159
117 dynamics in the classic world (Bevan, 2014). 160
118 These standardised containers were used 161
119 to transport large quantities of liquids and 162
120 other goods through a dense network of sea 163
121 and river routes. Maritime shipping was 164
122 the fastest and cheapest transport system so 165
123 amphorae were massively distributed over 166
124 the entire Roman empire. At the same 167
125 time amphorae were functional and robust 168
126 because they were designed to be trans- 169
127 ported aboard ships that may be cross- 170
128 ing hazardous waters. This robustness and 171
129 widespread use has allowed amphorae to 172
130 survive in higher quantities and frequencies 173
131 than containers serving a similar purpose 174
132 such as wooden barrels (Tchernia, 1986). 175

133 The study of these containers plays a key 176
134 role in our understanding of the Roman 177
135 economy thanks to their visibility in the 178
136 archaeological record (Greene, 1986, 162). 179
137 The production of an amphora type is typ- 180
138 ically linked to a specific area and prod- 181
139 uct so a trade link can be suggested be- 182

tween the production place of a type and
the sites where the amphorae of this type
are found. The aggregation of large vol-
umes of findings reveals the degree of spe-
cialisation of certain provinces that shipped
thousands of amphorae filled with a single
product to distant consumption places; this
dynamic can be seen in Baetica for olive
oil (Remesal Rodríguez, 1998; Funari, 1996)
and some areas of Italia for wine (Paterson,
1982; Loughton, 2003).

The use of this archaeological proxy also
presents some challenges. Elsewhere has
been argued that the information provided
by amphorae findings can be potentially bi-
ased by reuse activities (Peña, 2007, pp. 61-
208). These biases could affect distribution
patterns at least in two different aspects:
a) transportation to a new destination and
b) refill with a different substance than the
original.

The first scenario would see an empty
amphora refilled and shipped to a differ-
ent location. The archaeological record does
not allow us to track the route of the am-
phora which will always be found in the
last location it was shipped. This bias
would not heavily affect large-scale anal-
ysis such as the one we present here be-
cause the evidence for long-range reuse is
very scarce (Peña, 2007, p. 72). If short-
range reuse was frequent then the amphorae
found on nearby sites would be more homo-
geneous but it would not affect the role of
the dataset as proxy of long-range trade.

The second scenario would break univo-
cal ties between specific amphora types and
their contents. While this bias does not
affect the current work given our focus on
stamps it is certainly a relevant barrier to
improve our understanding of Roman trade
and requires further exploration (probab-
ly through residue analysis techniques, see

183 Pecci et al., 2017).
184 A significant percentage of these am-
185 phorae were stamped on one of their handles
186 with a code of letters and symbols. Most of
187 these codes are *tria nomina* identifying an
188 individual linked to trade activities, albeit
189 it is difficult to know if this person was in-
190 volved in the production of the container or
191 its contents (Remesal Rodríguez, 1998; Fu-
192 nari, 1996). In any case these codes high-
193 light the dynamics of trade because they
194 were not unique: amphorae found in dis-
195 tant sites were stamped with the same code
196 while containers found in the same place of-
197 ten exhibit a diversity of them. The study of
198 the frequencies of codes has found interest-
199 ing patterns on their spatiotemporal distri-
200 bution, and for this reason they seem a good
201 proxy for long-range trade in the classic
202 world (Remesal Rodríguez, 1998; Berni Mil-
203 let, 2008; Broekaert, 2015; Rubio-Campillo
204 et al., 2017).
205 This long tradition of amphora stamps
206 analysis has been mostly focused on sin-
207 gular sites or provinces. Here we use this
208 proxy to identify links within the Western
209 part of the Roman empire by comparing
210 the similarity of stamp codes found across
211 thousands of Roman sites. The hypothesis
212 to test can be defined as follows: sites re-
213 ceiving goods through different trade net-
214 works would be supplied by distinct pro-
215 ducers, so we should find differences in the
216 stamps found on these sites. In a majority
217 of sites only a small number of stamps has
218 been found, but if this hypothesis is cor-
219 rect then a large dataset should exhibit a
220 pattern significantly distinctive from a ran-
221 dom distribution of code stamps. In addi-
222 tion, if a group of provinces were more in-
223 tensely connected because they shared trade
224 routes then some code stamps should be
225 more present in these provinces than in the

226 rest of the areas.

The database used to test our working hypotheses is the Corpus of amphorae with Latin epigraphy compiled by the CEIPAC group over 30 years (Remesal Rodríguez et al., 2015). For each record in the dataset the following information was compiled: a) *id* of site where it was found, b) *province* where the archaeological site was located and c) stamp *code*. At present the Corpus contains 32.375 amphora stamps from which the amphorae collected in the city of Rome were removed for two reasons. First, the economic activities of the capital's supply were unique given its size and political role. Second, the amount of evidence collected in Rome is so large compared to the rest of the sites that the entire analysis would be biased towards this city. As a consequence the dynamics of the rest of the territory would be masked by the large weight of the capital. The remaining set of 24.092 stamps displayed 5.539 unique codes and is distributed over 1.278 sites covering a large percentage of Europe as depicted in Figure 1.

It is worth noting that around 25% of the stamps are not complete due to fragmentation or erosion. A previous study showed that the impact of this uncertainty in large-scale analysis was low (Rubio-Campillo et al., 2017). As a consequence we have integrated the fragmented stamps in the dataset without further issues.

The dataset contains a wide diversity of amphora types; nevertheless a majority of stamps has been found on Dressel 20 Baetican amphorae containing olive oil and Brindisian amphorae transporting olive oil or wine. The frequency distribution of the most popular amphorae types can be seen in Figure 2.

Figure 3 shows the heterogeneity of the



Figure 1: Spatial distribution of amphora stamps collected in the CEIPAC database. Most of the dataset comes from sites in the Western area of the Roman empire with the highest densities located at the Mediterranean coast and the provinces with strongest military presence (Britannia and Germania)

269 sample both in terms of number of sites per 284
 270 province and number of stamp codes per 285
 271 site. Provinces such as Italia, Narbonensis, 286
 272 and the two Germania have a large quantity 287
 273 of stamps spread over several sites while in
 274 most provinces less than 100 stamps were 288
 275 collected. The sites with a higher number
 276 of findings are located in the provinces with 289
 277 larger sample size while the sites in the rest
 278 of the provinces typically show less than 10 291
 279 code stamps. This pattern can be explained 292
 280 by a strong intensity bias as archaeologists 293
 281 working on some regions of Europe would 294
 282 have more interest in recording amphora 295
 283 stamps than areas where this type of stud-

ies is less common. The challenge then is to
 use appropriate methods able to detect spa-
 tial patterns despite this diversity of sample
 sizes.

3. Methods

The analysis of this dataset was per-
 formed in three steps: a) creation of a dis-
 similarity matrix between sites b) evalua-
 tion of province significance and c) identifi-
 cation of province clusters.

3.1. Jaccard distance matrix

Dissimilarity between two sites was based
 on the number of stamp codes that were

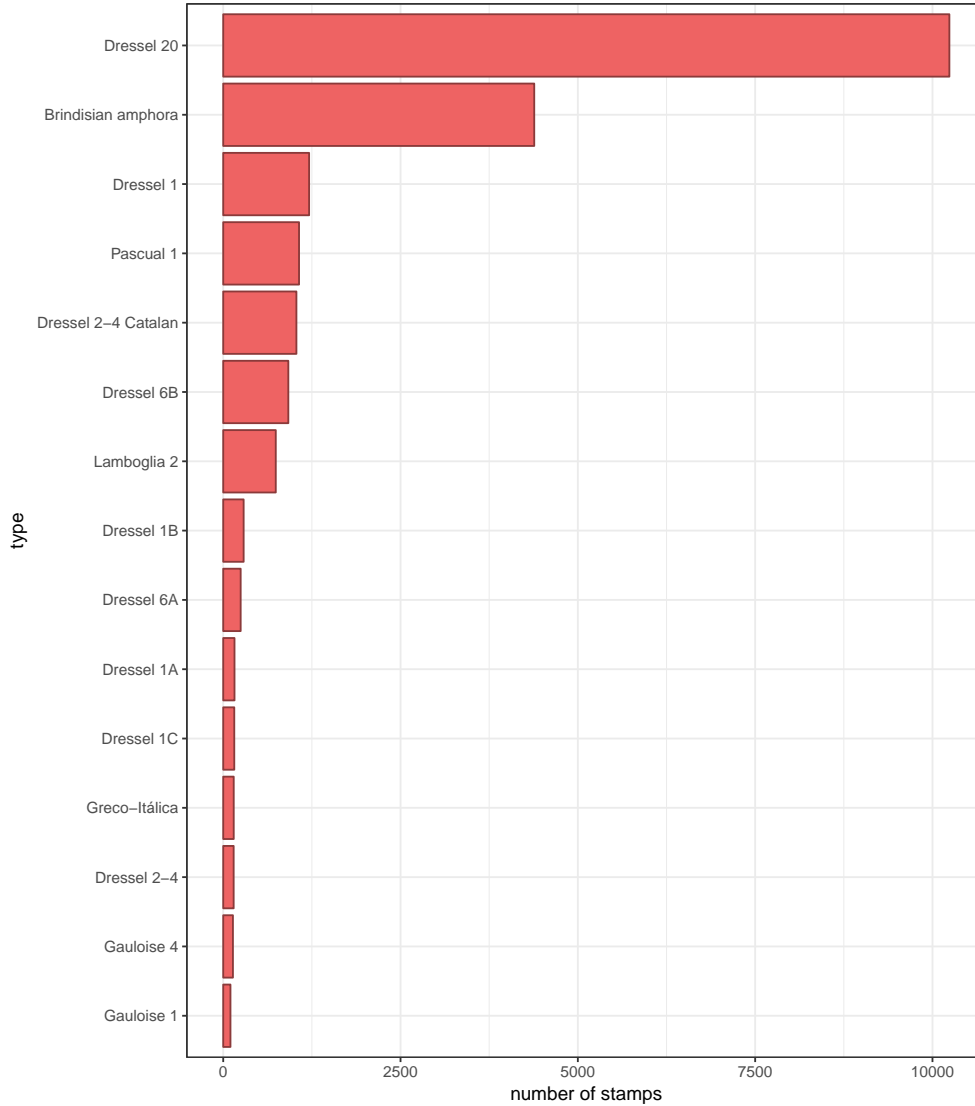


Figure 2: The CEIPAC database comprises a large diversity of containers with a total of 115 amphora types. This figure displays the frequency of the types having at least 100 stamps

297 present on one location and absent on the 305
 298 other one. This was quantified with a pop-
 299 ular similarity measure known as Jaccard 306
 300 distance. The distance between the sets of
 301 codes c_i and c_j collected in a pair of sites 307
 302 i and j is defined as the ratio between the 308
 303 number of codes found in both sites 309
 304 number of codes found at least in one site 310

as defined in Equation 1:

$$D_{Jaccard}(i, j) = 1 - \frac{|c_i \cap c_j|}{|c_i \cup c_j|} \quad (1)$$

311 The Jaccard distance is bounded between
 312 0 (i.e. the sites have exactly the same stamp
 codes) and 1 (i.e. the sites do not share
 any code). The pairwise computation of
 this index for the entire dataset generated a
 squared dissimilarity matrix of 1.278 rows

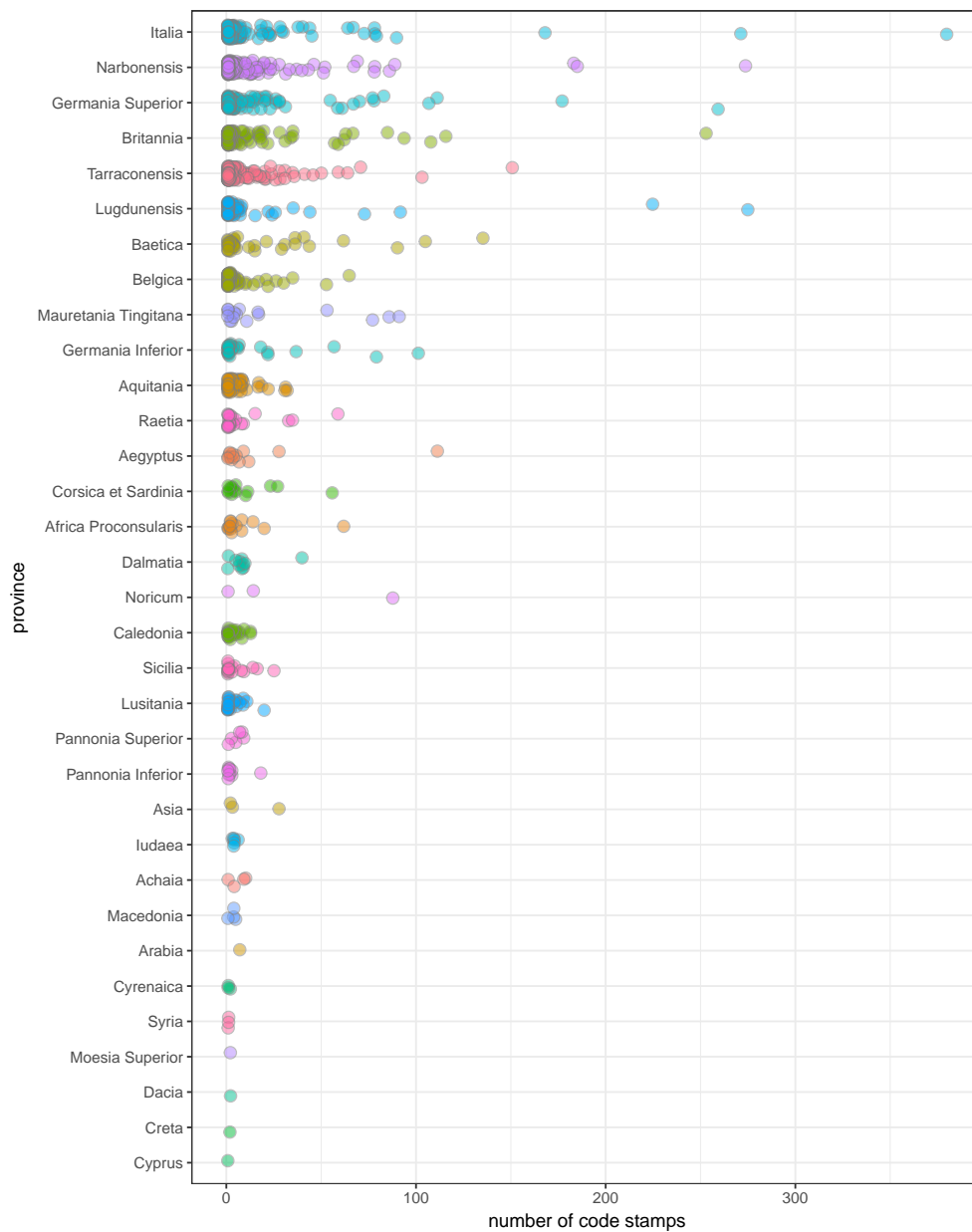


Figure 3: Distribution of sites based on its number of amphora code stamps (X axis) and province (Y axis). Each dot is a site and the provinces are sorted in decreasing order based on the total amount of stamps found on each province. Repetitions of the same stamp code on a site are counted only once

313 by 1.278 columns (i.e. number of sites).
 314 The average distance was close to 1 as most
 315 of the sites had a small number of unique
 316 stamps.

317 3.2. Multi-Response Permutation Procedure

318
 319 The second step required a comparison of
 320 the Jaccard distance between sites against
 321 their province. We estimated the signifi-
 322 cance of the first hypothesis by evaluating

323 the opposite *null* hypothesis: *The Jaccard* 366
 324 *distance between 2 sites is independent of* 367
 325 *their provincial attribution.* This is equiv- 368
 326 alent to compute the probability that two 369
 327 random sites from the entire dataset have a 370
 328 lower Jaccard distance than two sites ran- 371
 329 domly sampled from the same province; if 372
 330 this probability is low enough then we can 373
 331 reject the *null hypothesis*, thus suggesting 374
 332 that provincial structure played a role on 375
 333 trade routes.

334 The complex requirements of this test
 335 were met by the use of the Multi-Response
 336 Permutation Procedure (MRPP) (McCune
 337 and Grace, 2002; Mielke et al., 1976). 376
 338 MRPP was designed to analyse ecologi- 377
 339 cal datasets presenting similar challenges 378
 340 than the ones posed by archaeological data 379
 341 (e.g. fragmentation, noise, sampling bi- 380
 342 ases). First, MRPP does not assume any 381
 343 specific distribution of responses unlike sim- 382
 344 ilar methods such as MANOVA. Second, 383
 345 this approach allows to give different val- 384
 346 ues to the weight of each group in the fi- 385
 347 nal result. This was relevant in our analy- 386
 348 sis because the information of each province 387
 349 was not homogeneous as the number of sites 388
 350 per province was diverse (e.g. there were 389
 351 3 sites in Syria for 182 sites in Narbonen- 390
 352 sis). Finally, MRPP accepted Jaccard as a 391
 353 distance metric so no further data transfor- 392
 354 mations were required. Despite these ad- 393
 355 vantages to our knowledge the method has 394
 356 only been applied once in archaeological re- 395
 357 search (Rodgers, 1987). 396

358 MRPP evaluates the *null* hypothesis by 391
 359 comparing the average distance for the en- 392
 360 tire dataset against the average distance for 393
 361 elements of the same group (i.e. province) 394
 362 weighted by its sample size. It does so by 395
 363 performing random permutations between 396
 364 elements and assessing changes in this dis- 397
 365 tance. 398

For a set of provinces P and a set of stamp codes C_P the algorithm can be defined as follows:

1. compute the average Jaccard distance $\overline{D_p}$ between the sites of each province p in P .
2. compute the weight W_p of a province p based on the ratio between its number of sites s and the total number of sites in the sample:

$$W_p = \frac{s \in p}{\sum_{i=1}^P s \in i}$$

3. define an observed Delta value δ as the overall weighted mean of within-group means of distances:

$$\delta = \sum_{p=1}^P D_p W_p$$

4. permute the provinces associated with the different sites and compute δ again (this step is performed thousands of times).

The p-value is given by the percentage of permutations with δ lower or equal than the observed value computed in step 3. The algorithm also quantifies an effect size A suggesting the predictive power of the group (see McCune and Grace, 2002, for details).

3.3. Clustering

MRPP tests the statistical significance of the groups but it does not provide insights into the similarity between provinces. Our second hypothesis requires additional methods to group the provinces based on the stamp codes that can be found in their set of sites. This was achieved by creating a second matrix of mean within- and

399 between-province distances from the results 430
400 of the MRPP. The clustering algorithm 431
401 *neighbour joining* was then used to group 432
402 the provinces (Saitou and Nei, 1987). This 433
403 algorithm was chosen because it generates 434
404 an unrooted binary tree from a matrix of 435
405 dissimilarities without making any assump- 436
406 tions on the existence of a root node (which 437
407 did not exist in this case). The results could 438
408 then be visualised using a cladogram as a 439
409 means to evaluate what groups were created 440
410 by the method. 441

411 4. Results 442

412 The results of these methods were organ- 445
413 ised by the two original research questions. 446

414 4.1. Significance of the provincial structure 448

415 The application of the MRPP algorithm 449
416 generated the results that can be observed 450
417 in Table 1: 451

	value
p-value	< 0.001
observed δ	0.9974
within-province distance	0.9939
A	0.0035

Table 1: Results of MRPP using the entire sample 459

418 The observed average within-province 461
419 distance δ is consistently lower than the per- 462
420 mitted δ values. As a consequence the *null* 463
421 *hypothesis* that there is no relation between 464
422 the province of a site and its stamps has
423 a very low probability. However, the effect 465
424 size A is low despite the high significance of 466
425 the provincial structure. 467

426 The extreme diversity and sparsity of the 468
427 dataset causes all Jaccard distances to be 469
428 very high due to the low number of codes 470
429 found in a majority of sites. Hundreds of 471

430 sites have 5 or fewer codes so the probability
431 that two of these locations share one code
432 is very low, thus generating an A close to 0.
433 This issue is summarised in Figure 4 where
434 it is observed that the number of codes per
435 site is not normally distributed. A major-
436 ity of sites has one or two codes while the
437 shape has a very long tail due to a small
438 group of sites where hundreds of stamps
439 were recorded.

440 This uneven distribution of codes is prob-
441 ably caused by excavation biases as most
442 sites have not been fully excavated or have
443 not published all their findings. The large
444 number of sites with a small amount of
445 codes is adding noise to the general picture
446 by increasing the average Jaccard distances
447 between sites.

448 This impact can be explored by repeat-
449 ing MRPP for filtered datasets of sites hav-
450 ing at least a Minimum Number of Codes
451 (MNC). An iterative process was performed
452 with MNC values ranging from 1 to 100 (be-
453 ing MRPP with $MNC = 1$ equivalent to
454 the previous analysis). Results can be seen
455 in Figure 5

456 The signal given by A gradually intensi-
457 fies as we discard sites with a low number
458 of codes. It reaches a critical value an order
459 of magnitude higher than the previous re-
460 sult when MRPP is computed on sites with
461 at least 70 codes. The number of sites used
462 in the analysis is rather low at this point
463 and as a consequence A decreases again for
464 $MNC \geq 75$.

465 4.2. Provincial similarity 467

468 A given MNC value was required to
469 create the distance matrix of within- and
470 between- province dissimilarities. The
471 choice of MNC needed to balance the ef-
fect size A against the number of sites in-
involved in the analysis; if the value of MNC

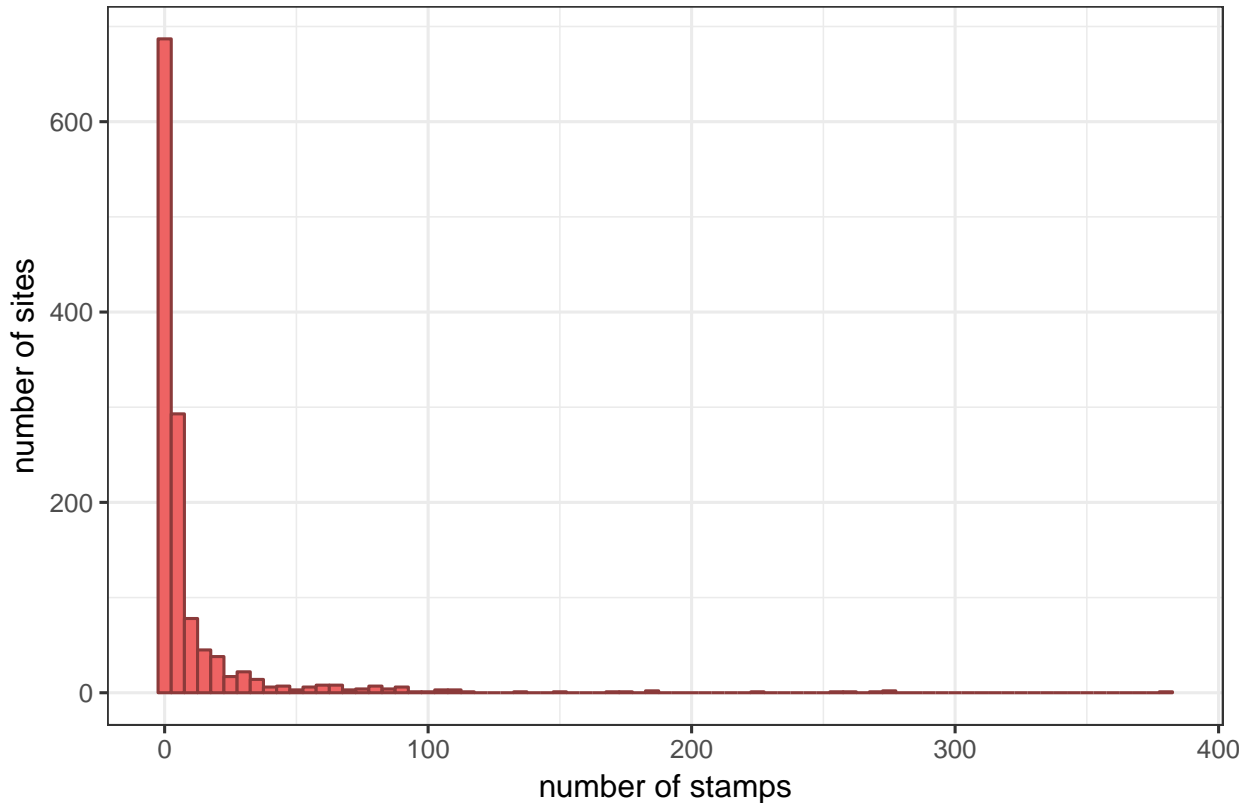


Figure 4: Histogram illustrating the number of code stamps per site with a bin width of 5. The distribution is extremely skewed with 800 sites containing less than 5 codes and a single site with 380 stamps (*Ostia Antica*)

472 was too low then it would contain a low 488
 473 signal-to-noise ratio while high MNC val- 489
 474 ues would limit the number of provinces 490
 475 used in the clustering because at least 2 sites 491
 476 per province are required. $MNC = 20$ was 492
 477 chosen as a compromise because it had a 493
 478 good effect size $A = 0.016$ and a reasonable 494
 479 number of 154 sites. The resultant distance 495
 480 matrix can be seen in Figure 6.

481 The matrix was used to generate the 497
 482 cladogram seen in Figure 7. Two clus- 498
 483 ters emerge from this visualisation: a group 499
 484 of tightly linked Mediterranean provinces 500
 485 and a second group comprising the north- 501
 486 ern *limes* of the Empire. 502

487 Additional analysis were conducted to ex-

488 plore the impact of parameter MNC and 489
 490 dataset variations in the final results. Sup- 491
 492 plementary Figure 1 shows the comparison 493
 494 of the cladograms reconstructed for differ- 495
 496 ent MNC values. This parameter explo- 497
 498 ration was performed from the complete 499
 500 dataset with $MNC = 1$ to the highest 501
 502 A value at $MNC = 75$. Supplementary 503
 504 Figure 2 displays cladograms on two dif-
 505 ferent subsets of the original dataset: a)
 506 stamps found on Dressel 20 amphorae and
 507 b) stamps found on other types of am-
 508 phorae. This exploration was required to
 509 assess if the predominance of Dressel 20
 510 in the dataset was responsible for the similar-
 511 ity patterns.

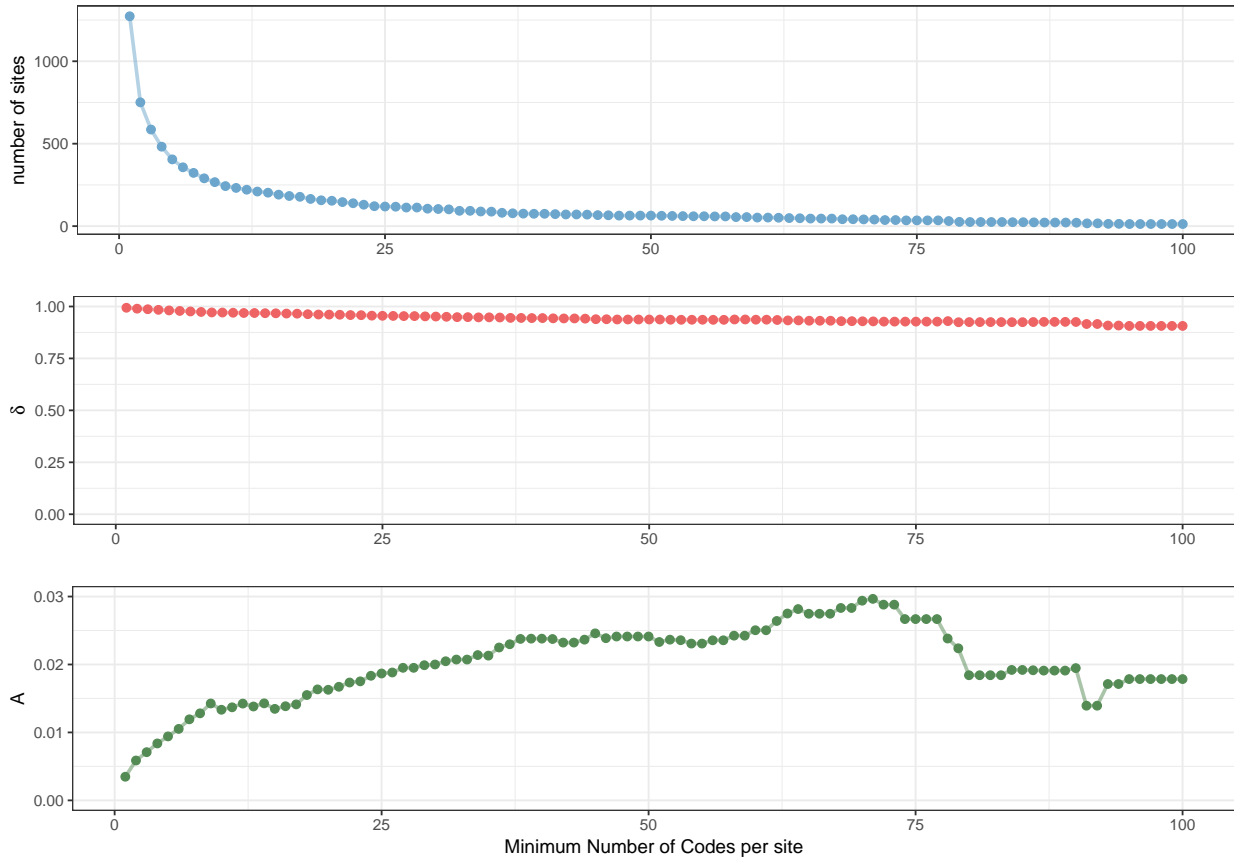


Figure 5: MRPP applied to filtered datasets. An MRPP has been performed to the collection of sites given by each MNC (X axis). The Y axis of the three graphs show: top) number of sites with given MNC, middle) average within-group distance or δ and bottom) effect size or A . The p-value for the entire dataset is consistently below 0.01

504 **Insert Supplementary 1 here** 517 military units on logistics or the relative in-
 505 **Supplementary 2 here** 518 tensity of multiple trade routes.

506 **5. Discussion**

507 The analysis revealed non-trivial patterns 521 where this site was located. It does not
 508 of distribution and these results confirm 522 mean that trade was organised independ-
 509 that amphora stamps are good proxies of 523 dently on every province, but it shows how
 510 long-range trade. First, provincial structure 524 distant regions of the Empire were supplied
 511 played an important role on the distribu- 525 by different trade networks based on their
 512 tion of liquid goods. Second, provinces that 526 code stamps. It is worth noting that a
 513 were supplied through the same network ex- 527 large percentage of the dataset is made by
 514 hibit higher similarity of stamp codes. Fi- 528 containers produced in specialised locations
 515 nally, the approach provides insight into a 529 such as the Dressel 20 olive oil amphorae
 516 diversity of factors including the impact of 530 in the Guadalquivir river (Mattingly, D.J.,

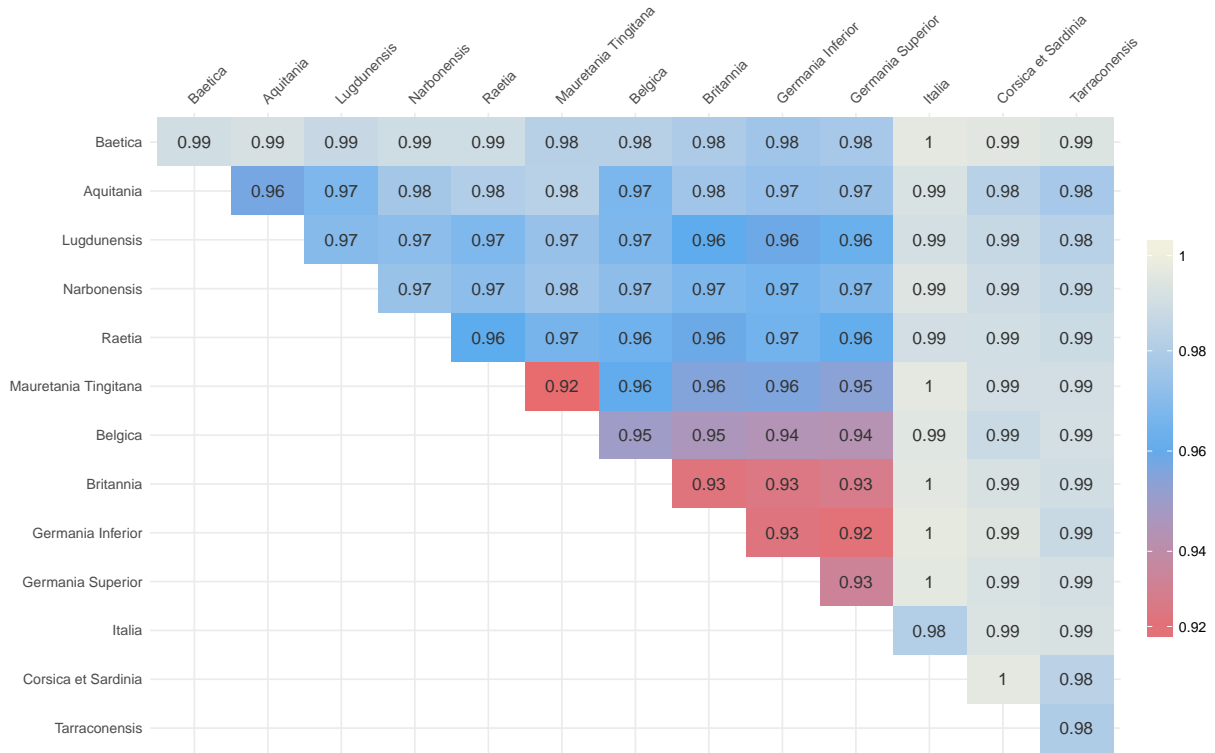


Figure 6: Distance matrix of mean within- and between- provincial distances for $MNC = 20$. Provinces with higher similarity are coloured in red tones while differences close to 1 are depicted in white

1988; Remesal Rodríguez, 1998). The workshops where these amphorae were made are located on a small segment of 20 kilometres along the riverside but they regularly shipped olive oil to different locations based on the code that was stamped on them. The patterns found on the distribution of stamps can only be caused by strong links between the workshops where the amphorae were made and the consumption places where they were found; if this relation did not exist then the result would be a random distribution over the Empire (so the *null* hypothesis would not be rejected).

The degree of provincial connectivity found in our dataset can mostly be explained by geographical distance. Good examples of this pattern are observed in the

clustering of most Western Mediterranean regions (Corsica and Sardinia, Italia, Tarraconensis and Baetica) and Northern Gallia (Lugdunensis and Aquitania). It is worth noting that this spatial structure has been derived from stamp similarity and no spatial data was used as input of the analysis.

This relation between spatial closeness and stamp similarity can be explained by a combination of similar trade routes and intense local trade, including the reuse and re-shipment of amphorae from local trade (Foley et al., 2012; Pecci et al., 2017). If future studies assess the relevance of amphorae reuse in Roman shipping then we will be able to improve even further our understanding of these similarities. In any case, the result appropriately captures the impor-



Figure 7: Similarity cladogram generated with neighbours joining algorithm for sites with $MNC = 20$

567 tance of Tobler's First Law of Geography in 576
 568 the case of economical dynamics: *everything* 577
 569 *is related to everything else, but near things* 578
 570 *are more related than distant things* (Tobler, 579
 571 1970).

572 Spatial closeness is the main driver of con-
 573 nectivity but the cladogram also shows two
 574 interesting exceptions to this general rule.
 575 The first one is the similarity of provinces

with strong military presence. The supply
 of the legions controlling the boundaries of
 the Roman Empire was one of the most
 important centres of demand for the em-
 pire (Scheidel et al., 2007, 575-576). The
 analysis shows the relevance of this factor
 as it breaks the pattern of spatial adja-
 cency by grouping provinces with intense
 military activity. Germania Superior, Ger-

585 mania Inferior and Britannia form the more 628
586 homogeneous group of the entire dataset 629
587 which suggests that the military units de- 630
588 ployed there received their olive oil and 631
589 wine supply from the same producers (Car- 632
590 reras Monfort and Funari, 1998). The clus- 633
591 ter is directly linked to Mauretania Tin- 634
592 gitana; this province is thousands of kilo- 635
593 metres apart from the northern group but 636
594 it is more similar to the provinces of the 637
595 German limes than to any other province, 638
596 including the entire Mediterranean. Mau- 639
597 retania was considered a frontier province 640
598 due to constant clashes between the Roman 641
599 army and local seminomad groups so mili- 642
600 tary units deployed here could have shared 643
601 the same trade network than the legions sta- 644
602 tioned 3000 kilometres north (Knight, 1991; 645
603 Cravioto, 2002; Pons Pujol, 2009). 646

604 The second pattern breaking Tobler's 647
605 law is the similarity of provinces over the 648
606 Atlantic-Rhine route. The four provinces 649
607 located along the course of the Rhine river 650
608 (Raetia, Germania Superior and Inferior) 651
609 are linked to Britannia and Belgica. In
610 contrast, Germania Superior and Germania
611 Inferior are distant from Gallia Narbonen-
612 sis which is the province where the Rhône 652
613 river ends its course into the Mediterranean 653
614 sea. This difference between the two rivers 654
615 suggests that the Atlantic route had more 655
616 intense long-range trade than the Rhine- 656
617 Rhône river route. This result provides 657
618 some insight into the current debate on 658
619 the route network that supplied the le- 659
620 gions garrisoning the German limes. On 660
621 the one hand, several authors point out 661
622 that the Atlantic route was too danger- 662
623 ous for the ships of this period while ma- 663
624 jor harbour structures have been found in 664
625 these two rivers (Fulford, 1992; Marlière, 665
626 2001). On the other hand, the Atlantic 666
627 route would have been used if ships were 667

able to safely move through the hazards of
the ocean (Remesal Rodríguez, 1986, 2008,
2010). If this option was possible then
the option would have been significantly
cheaper in terms of cost and time (Greene,
1986, 39-41). Recent archaeological works
are strengthening this hypothesis as they
have discovered evidence for large-scale har-
bour facilities in the Atlantic facade (Car-
reras Monfort and Morais, 2012; Morillo
et al., 2016). Our result supports this
new perspective by highlighting the simi-
larity of code stamps found in the Atlantic
provinces in contrast with the low simi-
larity between Germania and Narbonensis.
This result implies that the Rhine-Rhône
was not frequently used for long-range trade
but other authors have highlighted the rel-
evance of the Rhine-Rhône route for wine
barrels (Marlière, 2001). This opposite re-
sults could be explained by the lack of sta-
tistical testing methods or the fact that dif-
ferent containers may have followed a diver-
sity of routes.

The relevance of Baetican Dressel 20 am-
phorae in our dataset may also indicate that
this was the main product being shipped
through the Atlantic. Supplementary Fig-
ure 2 shows that this may be the case as
Narbonensis is close to Germania Superior
when the analysis excludes stamps found in
Dressel 20. However, this result is heav-
ily affected by sample size which forces us
to discard some key provinces without the
minimum number of sites (i.e. Germania
Inferior). In any case, our analysis sug-
gests that amphorae containing olive oil and
wine arrived to Germania and Belgica more
frequently through the Atlantic ocean than
through the Rhône-Rhine route.

6. Concluding remarks

The method presented here was able to answer the research questions while tackling the challenges posed by the complexity of the dataset. The combination of similarity indexes with a statistical permutation test has provided valuable insights into the dynamics of trade within the Roman Empire. This result also confirms the utility of amphora stamps as archaeological proxies of economic activity despite its high levels of uncertainty. For example, the ties between Mauretania Tingitana and the German limes was found despite the low volume of information currently available for Northern Africa (Teichner and Pons Pujol, 2008). This result showcases how this new approach is able to detect relevant signals of trade amongst the noise of fragmented archaeological data.

Nevertheless, the approach has limitations as any other method. First, the analysis is effective for large-scale resolutions and it would provide unreliable results in case of being applied at a lower scale, due to the need of large sample sizes. Additionally, we do not have any temporal information beyond amphora classifications and for this reason this analysis cannot be used to track change over time. This limit is defined by the dataset; the method could be extended by introducing temporal dynamics based on probabilistic approaches (Yubero-Gómez et al., 2016). However, the coarse scale of chronologies based on amphora classifications would possibly decrease the statistical robustness of the results.

Our approach could also be potentially complemented by spatial analysis for comparisons between stamp similarity and spatial closeness. This could strengthen the results but initial attempts based on Man-

tel tests suggested that spatial patterns were too sensitive to the uncertainty of this dataset. A quick glance to Figure 1 suggests a major impact of intensity and excavation biases over the analysed territory that would heavily affect any result obtained by pure spatial techniques.

The method presented here generates new opportunities for our understanding of the Roman economy despite these limitations. The same approach could be applied to identify differences in trade routes beyond provincial affiliation such as the existence of unique logistic networks for military or civilian sites, the use of different river routes over the territory or distinctive distributions of amphora types. The combination of similarity distances with statistical tests also opens the door to comparative analysis between the routes followed by different goods and types of containers. The use of other proxies is important because amphora is the most visible archaeological proxy for long-range trade and by its very own nature its importance can overemphasize provincial connectivity (Woolf, 1992). The analysis of goods more vulnerable to postdepositional processes such as textiles may provide a different perspective by highlighting the complexity and diversity of Roman trade (Greene, 1986, 13-15).

The last years have seen a dramatic increase in the quantity and quality of datasets on the Roman empire, but data does not automatically transform into knowledge. This work illustrates the current need for hypothesis testing in the study of past economies. Quantitative analysis is not as common in Roman archaeology as it is in other archaeological fields where statistics have been regularly applied for decades (Thomas, 1978). The study of Roman economy needs appropriate quantita-

753 tive methods able to tackle the challenges 793
754 posed by archaeological evidence in order 794
755 to identify meaningful patterns in complex 795
756 datasets (Bevan, 2015). The field needs 796
757 to move forward from basic exploratory 797
758 data analysis towards the use of new frame- 798
759 works able to test specific working hypothe- 800
760 ses. This combination of new datasets and 801
761 methods is the only way to answer the big 802
762 questions of the field and advance in our un- 803
763 derstanding of the complexities of the clas- 804
764 sic world. 805

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774 boundaries were based on the work of An- 815
775 cient World Mapping Center (2016). All 816
776 analysis have been performed in R using 817
777 the libraries *vegan*, *ggtree* and *ggplot2* (Ok- 818
778 sanen et al., 2007; Yu et al., 2017; Wickham, 819
779 2009). 820

780 Source code and datasets are available 821
781 under Open licenses and can be freely acces- 822
782 sible from [https://github.com/xrubio/](https://github.com/xrubio/ecologyStamps) 823
783 [ecologyStamps](https://github.com/xrubio/ecologyStamps). 824

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787 and XRC performed the analysis. XRC 828
788 wrote the paper. 829

789 References 830

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